# **Coordinate Geometry**

## 2016

#### Short Answer Type Questions I [2 Marks]

## **Question 1.**

Find the ratio in which y-axis divides the line segment joining the points A(5, -6) and B(-I, -4). Also find the coordinates of the point of division.

#### Solution:

Let the point on y-axis be P(0, y) and AP : PB = k : 1.  $\therefore$  Co-ordinates of P given by:  $\left(\frac{mx_2 + nx_1}{m + n}, \frac{my_2 + ny_1}{m + n}\right)$ Then, taking x-axis of A, B;  $\frac{5 \times 1 + k(-1)}{k + 1} = 0 \implies \frac{5 - k}{k + 1} = 0 \implies k = 5$ Hence the required ratio is 5 : 1 Now, taking y-axis,  $y = \frac{(-4)(5) + (1)(-6)}{5 + 1} = \frac{-13}{3}$ Hence point on y-axis is  $\left(0, \frac{-13}{3}\right)$ 

#### **Question 2**.

The x-coordinate of a point P is twice its y-coordinate. If P is equidistant from Q(2, -5) and R(-3, 6), find the coordinates of P.

#### Solution:

Let the required point be (2y, y). Let Q(2, -5) and R(-3, 6) are given points. Now,  $PQ = PR \Rightarrow \sqrt{(2y-2)^2 + (y+5)^2} = \sqrt{(2y+3)^2 + (y-6)^2}$ [:: using Distance formula,  $\sqrt{(x-2)^2 + (y+5)^2} = \sqrt{(x+3)^2 + (y-6)^2}$ ] Squaring both sides we get  $4y^2 + 4 - 8y + y^2 + 10y + 25 = 4y^2 + 9 + 12y + y^2 - 12y + 36$   $\Rightarrow 2y + 29 = 45$   $\Rightarrow 2y = 45 - 29 = 16$   $\Rightarrow y = 8$   $\Rightarrow 2y = 16$ Hence coordinates of P are (16, 8)

#### **Question 3.**

Let P and Q be the points of trisection of the line segment joining the points A(2, -2) and B(-7, 4) such that P is nearer to A. Find the coordinates of P and Q.

## Solution:

Let A(2, -2), B(-7, 4) be given points. Let P(x, y), Q(x', y') are point of trisection.

A P Q (2, -2) B (-7, 4) P divides AB in the ratio 1:2 Coordinates of P are  $\left(\frac{2 \times 2 + 1(-7)}{1+2}, \frac{(-2)(2) + 1(4)}{1+2}\right)$  or (-1, 0)

Q is mid point of PB. So using mid point formula coordinates of Q are  $\left(\frac{-1-7}{2}, \frac{0+4}{2}\right)$  or (-4, 2)

CLICK HERE

#### **Question 4.**

Prove that the points (3,0), (6,4) and (-1,3) are the vertices of a right angled isosceles triangle.

#### Solution:

Let the triangle be  $\triangle ABC$  as shown in figure. Distances are: A(3, 0) Using distance formula,  $AB = \sqrt{(3-6)^2 + (0-4)^2} = 5$ BC =  $\sqrt{(6+1)^2 + (4-3)^2} = 5\sqrt{2}$  $CA = \sqrt{(-1-3)^2 + (3-0)^2} = 5$ Here,  $AB = AC \implies \triangle ABC$  is isosceles triangle  $AB^{2} + AC^{2} = (5)^{2} + (5)^{2} = 25 + 25 = 50$ Consider. B(6, 4) C(-1, 3) and,  $BC^2 = (5\sqrt{2})^2 = 50$ ⇒ Here,  $AB^2 + AC^2 = BC^2$ *:*..  $\Rightarrow \Delta ABC$  is a right angled triangle.

[:: In right  $\Delta$ , using Pythagoras theorem (H)<sup>2</sup> = (P)<sup>2</sup> + (B)<sup>2</sup>] where H = hypotenuse, B = base, P = perpendiculars

#### **Question 5.**

Find the ratio in which the point (-3, k) divides the line-segment joining the points (-5, -4) and (-2,3). Also find the value of k.

Solution:



#### **Question 6.**

Prove that the points (2, -2), (-2, 1) and (5, 2) are the vertices of a right angled triangle. Also find the area of this triangle.

## Solution:



**CLICK HERE** 

### Short Answer Type Questions II [3 Marks]

#### **Question 7.**

In figure ABC is a triangle coordinates of whose vertex A are (0, -1). D and E respectively are the mid-points of the sides AB and AC and their coordinates are (1, 0) and (0,1) respectively. If F is the mid-point of BC, find the areas of  $\triangle$ ABC and  $\triangle$ DEF.

## Solution:

. Let coordinates of B are (x, y). Then using mid point formula we

$$\frac{x+0}{2} = 1 \qquad \Rightarrow x = 2$$
$$\frac{y-1}{2} = 0 \qquad \Rightarrow y = 1$$

Coordinates of B are (2,1)

Let coordinates of C are (p, q)

Similarly coordinates of C we have

$$\frac{p+0}{2} = 0 \qquad \Rightarrow p = 0$$
$$\frac{q-1}{2} = 1 \qquad \Rightarrow q = 3$$

Coordinates of C are (0, 3)

Area of **ABC** 

$$\Rightarrow \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = \frac{1}{2} [0(1 - 3) + 2(3 + 1) + 0(-1 - 1)]$$
$$= \frac{1}{2} \times 8 = 4 \text{ sq. units}$$

Coordinates of F are  $\left(\frac{2+0}{2}, \frac{1+3}{2}\right)$  i.e. (1, 2) [:: Using mid-point formula] Area of  $\triangle DEF = \frac{1}{2}[1(1-2) + 0(2-0) + 1(0-1)] = \frac{1}{2}[-1+0-1]$  $= \frac{1}{2} \times (-2) = [-1] = 1$  sq. units [:: Area cannot be negative]





## **Question 8.**

If the point P(x, y) is equidistant from the points A (a + b, b – a) and B(a -b,a+ b). Prove that bx = ay.

## Solution:



## **Question 9.**

If the point C(-I, 2) divides internally the line-segment joining the points A(2, 5) and B(x,y) in the ratio 3 : 4, find the value of  $x^2 + y^2$ .

## Solution:

Using section formula,



1

Similarly.

Hence;  $x^2 + y^2 = (-5)^2 + (-2)^2 = 25 + 4 = 29$ 

#### Long Answer Type Questions [4 Marks]

#### **Question 10.**

Prove that the area of a triangle with vertices (t, t - 2), (t + 2, t + 2) and (t + 3, t) is independent of t.

## Solution:

Given vertices of triangle are  $\{t, t-2\}, \{t+2, t+2\}, \{t+3, t\}$ Let  $(x_1, y_1), (x_2, y_2), (x_3, y_3)$  are vertices of the triangle. Area of the triangle  $= \frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$   $= \frac{1}{2}[t(t+2-t) + (t+2)\{t-t+2\} + (t+3)\{t-2-t-2\}]$   $= \frac{1}{2}[2t+2t+4-4t-12]$   $= \frac{1}{2} \times (-8) = 4$  sq units, since area can't be negative. Hence, area is independent of t.

**CLICK HERE** 

🕀 www.studentbro.in

## **Question 11.**

In fig., the vertices of AABC are A(4, 6), B(I, 5) and C(7, 2). A line-segment DE is drawn to intersect the sides AB and AC

at D and E respectively such that AD/AC=AE/AC=1/3. Calculate the area of  $\Delta$ ADE and compare it with area of  $\Delta$ ABC.

Solution:

 $\frac{AD}{AB} = \frac{1}{3}$ 3AD = ABL\_\_\_\_\_ B(1, 5) Given: 3AD = AD + DB*.*.. 2AD = DB $\frac{AD}{DB} = \frac{1}{2}$  $\frac{AE}{EC} = \frac{1}{2}$ Similarly. Calculated using section formula Coordinates of D are  $\left(\frac{1(1)+2(4)}{1+2}, \frac{1(5)+2(6)}{1+2}\right)$  i.e.  $\left(3, \frac{17}{3}\right)$ Coordinates of E are  $\left(\frac{1(7)+2(4)}{1+2}, \frac{1(2)+z(6)}{1+2}\right)$  i.e.  $\left(5, \frac{14}{3}\right)$ Area of  $\triangle ADE = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$  $= \frac{1}{2} \left[ 4 \left( \frac{17}{3} - \frac{14}{3} \right) + 3 \left( \frac{14}{3} - 6 \right) + 6 \left( 6 - \frac{17}{3} \right) \right]$  $= \frac{1}{2} \left[ 4 + 3\left(\frac{-4}{3}\right) + 5\left(\frac{1}{3}\right) \right]$  $=\frac{1}{2}\left[4-4+\frac{5}{3}\right]=\frac{5}{6}$  sq. units Area of  $\triangle ABC = \frac{1}{2}[4(5-2) + 1(2-6) + 7(6-5)]$  $= \frac{1}{2} [4 \times 3 + (-4) + 7 \times 1]$  $=\frac{1}{2}[12-4+7]$  $=\frac{1}{2} \times 15 = \frac{15}{2}$  sq. units  $\frac{\text{Area}\,(\Delta \text{ADE})}{\text{Area}\,(\Delta \text{ABC})} = \frac{5/6}{15/12} = \frac{5}{6} \div \frac{15}{12} = \frac{5}{6} \times \frac{12}{15} = \frac{2}{3}$ Hence, A(4, 6)

Get More Learning Materials Here :

B(1, 5)

C(7, 2)

## **Question 12.**

The coordinates of the points A, B and C are (6,3), (-3,5) and (4, -2) respectively.P(JC, y) is

$$\frac{\operatorname{ar}\left(\Delta \operatorname{PBC}\right)}{\operatorname{ar}\left(\Delta \operatorname{ABC}\right)} = \left|\frac{x+y-2}{7}\right|.$$

any point in the plane. Show that

## Solution:

Taking points P, B, C. Firstly,

$$\operatorname{area}(\Delta PBC) = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
$$= \frac{1}{2} [x(7) - 3(-2 - y) + 4(y - 5)]$$
  
$$= \frac{1}{2} [7x + 7y - 14] \text{ sq. units}$$
  
Now,  
$$\operatorname{area}(\Delta ABC) = \frac{1}{2} [6 \times 7 - 3(-5) + 4(3 - 5)]$$
  
$$= \frac{1}{2} [42 + 15 - 8] = \frac{1}{2} \times 49 \text{ sq. units}$$
  
Hence,  
$$\left| \frac{\operatorname{area}(\Delta PBC)}{\operatorname{area}(\Delta ABC)} \right| = \left| \frac{7x + 7y - 14}{49} \right| = \left| \frac{x + y - 2}{7} \right|$$

**Question 13.** 

Find the area of the quadrilateral ABCD, the coordinate of whose vertices are A(1, 2), B(6,2), C(5,3) and D(3,4).

### Solution:

Area of 
$$\triangle ABC = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  

$$= \frac{1}{2} [1(2 - 3) + 6(3 - 2) + 5(2 - 2)]$$

$$= \frac{1}{2} [-1 + 6 + 0] = \frac{5}{2} \text{ sq. units}$$
Now, Area of  $(\triangle ACD) = \frac{1}{2} [1(3 - 4) + 5(4 - 2) + 3(2 - 3)]$   

$$= \frac{1}{2} [-1 + 10 - 3]$$

$$= \frac{1}{2} [-1 + 10 - 3]$$

$$= \frac{1}{2} \times 6 = 3 \text{ sq. units}$$
Hence, Area (quadrilateral ABCD) =  $\frac{5}{2} + 3 = \frac{11}{2} \text{ sq. units}$ 

Hence, Area (quadrilateral ABCD) =  $\frac{1}{2} + 3 = \frac{1}{2}$  sq. units

## **Question 14.**

Find the area of a quadrilateral ABCD, the coordinates of whose vertices are A(-3,2), B(5,4), C(7, -6) and D(-5, -4).

## Solution:

Area of 
$$\triangle ABD = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  

$$= \frac{1}{2} [-3(8) + 5(-6) + (-5) (2 - 4)]$$

$$= \frac{1}{2} [-24 - 30 + 10]$$

$$= \frac{1}{2} \times (-44) = (-22) = 22 \text{ sq. units}$$
ea can't be negative  
area of  $\triangle BCD = \frac{1}{2} [5(-2) + 7 (-8) - 5(10)]$ 

Since are

area of 
$$\triangle BCD = \frac{1}{2} [5(-2) + 7(-8) - 5(10)]$$

Get More Learning Materials Here : 📕

# Regional www.studentbro.in

$$= \frac{1}{2} [-10 - 56 - 50]$$
  
=  $\frac{1}{2} (-116) = (-58) = 58$  sq. units

Since area cannot be negative.

Area of quadrilateral ABCD = Area ( $\triangle$ ABD) + area ( $\triangle$ BCD) = 22 + 58 = 80 sq. units.

#### 2015

#### Short Answer Type Questions I [2 Marks]

#### **Question 15.**

If A(5, 2), B(2, -2) and C(-2, t) are the vertices of a right angled triangle with  $\angle B = 90^{\circ}$ , then find the value of t.

## Solution:

Using distance formula in right triangle ABC,  $AB^{2} = (5-2)^{2} + (2-(-2))^{2} = 9 + 16 = 25$  $AC^{2} = (5 - (-2))^{2} + (2 - t)^{2} = 49 + 4 - 4t + t^{2} = t^{2} - 4t + 53$  $BC^{2} = (2+2)^{2} + (-2-t)^{2} = 16 + t^{2} + 4t + 4 = t^{2} + 4t + 20$ Now  $\triangle ABC$  is a right triangle, right angled at B.  $AC^2 = AB^2 + BC^2$ So,  $t^2 - 4t + 53 = 25 + t^2 + 4t + 20$  $8t = 8 \implies t = \frac{8}{8} = 1$ Hence, t = 1Denni A(5, 2) 90 B(2, -2) C(-2, t)

(By Pythagoras theorem)

#### **Question 16.**

Find the ratio in which the point P P(3/4,5/12) divides the line segment joining the points A(1/2,3/2) and 3(2, -5).

## Solution:

Let point P divides the line segment AB in the ratio k : 1. Using section formula,

then the coordinates of P	$\operatorname{are}\left(\frac{2k+\frac{1}{2}}{k+1}, \frac{-5k+\frac{3}{2}}{k+1}\right)$	K a)	$P\left(\frac{3}{4}, \frac{5}{12}\right)$ B(2, -5)
A.T.Q.	$\frac{2k+\frac{1}{2}}{k+1} = \frac{3}{4}$	$A\left(\frac{1}{2},\frac{5}{2}\right)$	
$\Rightarrow$	8k+2 = 3k+3		
⇒	5k = 1		
⇒	$k = \frac{1}{5}$		
Hence P divides the line	segment AB in the ratio 1 · 5		

Hence, P divides the line segment AB in the ratio 1:5.

## Question 17.

The points A(4,7), B(p, 3) and C(7,3) are the vertices of a right triangle, right-angled at B. Find the value of p. **Solution:** 

**CLICK HERE** 

Get More Learning Materials Here :



## Question 18.

Find the relation between x and y if the points A(x, y), B(-5, 7) and C(-4, 5) are collinear **Solution:** 

∴ A, B and C are collinear. So, area (
$$\triangle ABC$$
) = 0  
∴  $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$   
⇒  $\frac{1}{2}[x(7 - 5) + (-5)(5 - y) + (-4)(y - 7)] = 0$   
 $2x - 25 + 5y - 4y + 28 = 0$   
⇒ Required relation between x & y is  $2x + y + 3 = 0$ 

## Question 19.

If A(4,3), B(-l,y) and C(3,4) are the vertices of right triangle ABC, right-angled at A, then find the value of y.

0

#### Solution:



## Question 20.

Show that the points (a,a), (-a,-a) and ( $-\sqrt{3}a$ ,  $\sqrt{3}a$ ) are the vertices of an equilateral triangle. **Solution:** 

**CLICK HERE** 

Let P(a, a), Q(-a, -a), R(
$$-\sqrt{3}a, \sqrt{3}a$$
). Using distance formula,  
PQ =  $\sqrt{(a+a)^2 + (a+a)^2} = \sqrt{4a^2 + 4a^2} = 2\sqrt{2}a$   
QR =  $\sqrt{(-a+\sqrt{3}a)^2 + (-a-\sqrt{3}a)^2}$   
=  $\sqrt{a^2 + 3a^2 - 2\sqrt{3}a^2 + a^2 + 3a^2 + 2\sqrt{3}a^2} = \sqrt{8a^2} = 2\sqrt{2}a$   
RP =  $\sqrt{(a+\sqrt{3}a)^2 + (a-\sqrt{3}a)^2}$   
=  $\sqrt{a^2 + 3a^2 + 2\sqrt{3}a^2 + a^2 + 3a^2 - 2\sqrt{3}a^2} = \sqrt{8a^2} = 2\sqrt{2}a$   
 $\Rightarrow$  Here, PQ = QR = RP  
 $\Rightarrow$  P  $\cap$  R are vertices of an equilatoral triangle

... P, Q, R are vertices of an equilateral triangle.

For what values of k are the points (8,1), (3, -2k) and (k, -5) collinear? **Solution:** 

For collinear points area of  $\Delta$  made by these points will be zero.

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$\Rightarrow \qquad 8(-2k + 5) + 3(-5 - 1) + k(1 + 2k) = 0$$

$$\Rightarrow \qquad -16k + 40 - 18 + k + 2k^2 = 0$$

$$2k^2 - 15k + 22 = 0$$

$$2k^2 - 11k - 4k + 22 = 0$$

$$k(2k - 11) - 2(2k - 11) = 0$$

$$(2k - 11)(k - 2) = 0$$

$$\Rightarrow \qquad k = 2, k = \frac{11}{2}$$

#### Short Answer Type Questions II [3 Marks]

## Question 22.

Find the area of the triangle ABC with A(I, -4) and mid-points of sides through A being (2, -1) and (0, -1).

## Solution:



### Question 23.

Find the area of the triangle PQR with Q (3, 2) and the mid-points of the sides through Q being (2, -1) and (1,2).

## Solution:





#### Question 24.

If the coordinates of points A and B are (-2, -2) and (2, -4) respectively, find the coordinates of P such that AP = 3/7 AB, where P lies on the line segment AB. **Solution:** 

**CLICK HERE** 

$$A(-2, -2) \qquad (x, y) \qquad B(2, -4)$$

$$AP = \frac{3}{7} AB \Rightarrow AP : PB = 3 : 4$$

Given,

$$\Rightarrow$$
 P divides AB in the ratio 3 :  
Using section formula,

Coordinates of point P are = 
$$\left(\frac{3 \times 2 + 4 \times (-2)}{3 + 4}, \frac{3 \times (-4) + 4 \times (-2)}{3 + 4}\right) = \left(\frac{-2}{7}, \frac{-20}{7}\right)$$

Question 25.

Find the coordinates of a point P on the line segment joining A(l, 2) and B(6,7) such that AP=2/5AB

Solution:

 $A(1,2) \qquad P \qquad B(6,7)$   $AP = \frac{2}{AB}$ 

Given,

*.*:.

$$AP : PB = 2:3 \Rightarrow P$$
 divides AB in ratio 2:3

Using section formula,

Coordinates of point P are 
$$\left(\frac{2 \times 6 + 3 \times 1}{2 + 3}, \frac{2 \times 7 + 3 \times 2}{2 + 3}\right)$$
 i.e. (3, 4)

.: Coordinates of P are (3, 4)

## **Question 26.**

Point A lies on the line segment PQ joining P(6, -6) and Q(-4, -1) in such a way that PA/PQ=2/5. If point P also lies on the line 3x + k(y + 1) = 0, find the value of k

#### Solution:

Coordinates of P are (6, -6). Given that:

P(6, -6) lies on the line. So,3x + k(y + 1) = 0 $\Rightarrow 3 \times 6 + k(-6 + 1) = 0$  $\Rightarrow 18 - 5k = 0$  $\Rightarrow k = \frac{18}{5}$ 

## Long Answer Type Questions [4 Marks]

#### Question 27.

If A(-4,8), B(-3, -4), C(0, -5) and D(5,6) are the vertices of a quadrilateral ABCD, find its area.

#### Solution:

Firstly, 
$$\operatorname{ar}(\Delta ABC) = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
 $= \frac{1}{2} [-4(-4 + 5) - 3(-5 - 8) + 0(8 + 4)]$   
 $= \frac{1}{2} [-4 + 39 + 0] = \frac{1}{2} \times 35$   
 $= \frac{35}{2} \operatorname{sq. units}$   
Now,  $\operatorname{ar}(\Delta ACD) = \frac{1}{2} [-4(-5 - 6) + 0(6 - 8) + 5(8 + 5)]$   
 $= \frac{1}{2} [44 + 0 + 65] = \frac{109}{2} \operatorname{sq. units}$   
So,  $\operatorname{ar}(\operatorname{quadrilateral} ABCD) = \operatorname{ar}(\Delta ABC) + \operatorname{ar}(\Delta ACD)$   
 $= \frac{35}{2} + \frac{109}{2} = \frac{144}{2} = 72 \operatorname{sq. units}$ 

## Question 28.

If P(-5, -3), Q (-4, -6), R(2, -3) and S(I, 2) are the vertices of a quadrilateral PQRS, find its area.

Solution:

Firstly, 
$$\operatorname{ar}(\Delta PQR) = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
 $= \frac{1}{2} [-5(-6 + 3) - 4(-3 - 3) + 2(-3 + 6)]$   
 $= \frac{1}{2} [15 + 0 + 6] = \frac{21}{2} \operatorname{sq. units}$   
Now,  $\operatorname{ar}(\Delta PRS) = \frac{1}{2} [-5(-3 - 2) + 2(2 + 3) + 1(-3 + 3)]$   
 $= \frac{1}{2} [25 + 10 + 0] = \frac{35}{2} \operatorname{sq. units}$   
So,  $\operatorname{ar}(\operatorname{quad} PQRS) = \operatorname{ar}(\Delta PQR) + \operatorname{ar}(\Delta PRS)$   
 $= \frac{21}{2} + \frac{35}{2} = \frac{56}{2} = 28 \operatorname{sq. units}.$ 

## Question 29.

Find the values of k so that the area of the triangle with vertices (1, -1), (-4, 2k) and (-k, -5) is 24 sq. units.

Solution:

Given that, Area of  $\Delta = 24$  sq. units

$$\Rightarrow \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| = 24 |1(2k + 5) - 4(-5 + 1) - k(-1 - 2k)| = 48 \Rightarrow |2k + 5 + 16 + k + 2k^2| = 48 \Rightarrow |2k^2 + 3k + 21| = 48 \Rightarrow |2k^2 + 3k + 21 = \pm 48 \Rightarrow 2k^2 + 3k + 21 = 48 2k^2 + 3k - 27 = 0 2k^2 + 9k - 6k - 27 = 0 k(2k + 9) - 3(2k + 9) = 0 (2k + 9)(k - 3) = 0 \\ \Rightarrow |2k^2 + 9k - 6k - 27 = 0 \\ (2k + 9)(k - 3) = 0 \\ \Rightarrow |2k^2 + 9k - 6k - 27 = 0 \\ (2k + 9)(k - 3) = 0 \\ \Rightarrow |2k^2 + 9k - 6k - 27 = 0 \\ (2k + 9)(k - 3) = 0 \\ \vdots |2k^2 + 3k + 21 = -48 \\ 2k^2 + 3k + 21 = -48 \\ 2k^2 + 3k + 21 = -48 \\ 2k^2 + 3k + 69 = 0 \\ Discriminant, D = (3)^2 - 4 \times 2 \times 69 [\because b^2 - 4ac] \\ = -ve \\ \therefore No solution \\ \Rightarrow |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0 \\ \vdots |2k + 9|(k - 3) = 0$$

## **Question 30.**

Find the values of k for which the points A(k + 1, 2k), B(3k, 2k + 3) and C(5k - 1, 5k) are collinear.

CLICK HERE

>>

R www.studentbro.in

Solution:

∴ The points A(k + 1, 2k), B(3k, 2k + 3) and C(5k - 15k) are collinear. So, ar (△ABC) = 0  

$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$\frac{1}{2}[(k + 1)(2k + 3 - 5k) + 3k(5k - 2k) + (5k - 1)(2k - 2k - 3)] = 0$$

$$\Rightarrow \qquad (k + 1)(-3k + 3) + 3k \times 3k + (5k - 1)(-3) = 0$$

$$\Rightarrow \qquad (k + 1)(-3k + 3) + 3k \times 3k + (5k - 1)(-3) = 0$$

$$\Rightarrow \qquad -3k^2 + 3k - 3k + 3 + 9k^2 - 15k + 3 = 0$$

$$\Rightarrow \qquad 6k^2 - 15k + 6 = 0$$

$$\Rightarrow \qquad 2k^2 - 5k + 2 = 0$$

$$2k^2 - 4k - k + 2 = 0$$

$$2k(k - 2) - 1(k - 2) = 0$$

$$\Rightarrow \qquad (k - 2)(2k - 1) = 0$$

$$\Rightarrow \qquad k = 2 \text{ or } k = \frac{1}{2}.$$

## Question 31.

The base BC of an equilateral triangle ABC lies on y-axis. The coordinates of point C are (0, -3). The origin is the mid-point of the base. Find the coordinates of the points A and B. Also find the coordinates of another point D such that BACD is a rhombus.

## Solution:

Given that,  $\therefore$  O is mid point of BC and coordinates of C are (0, -3)

∴ coordinate of B are (0, 3)

Now AO will be the perpendicular bisector of BC. Therefore A will lie on x-axis. let coordinates of A are (x, 0)

Now, in equilateral  $\triangle ABC$ , AB = BC

Using distance formula,

$$\Rightarrow \qquad \sqrt{(x-0)^2 + (0-3)^2} = 6$$
$$\sqrt{x^2 + 9} = 6$$
$$x^2 + 9 = 36 \Rightarrow x^2 = 27$$



$$x = \pm 3\sqrt{3}$$

 $\therefore$  coordinates of A are  $(3\sqrt{3}, 0)$  or  $(-3\sqrt{3}, 0)$ 

When A is  $(3\sqrt{3}, 0)$  then D will be  $(-3\sqrt{3}, 0)$  so that BACD is a rhombus, since opposite sides are equal.

#### 2014

### Short Answer Type Questions II [3 Marks]

## Question 32.

If the point A(0, 2) is equidistant from the points B(3, p) and C(p, 5), find p. Also find the length of AB.

## Solution:





## Question 33.

If the points A(-2,1), B (a, b) and C(4, -1) are collinear and a - b = 1, find the value of a and b.

#### Solution:

Since, the points A(-2, 1), B(a, b) and C(4, -1) are collinear, So, area of triangle,  $ar(\Delta ABC) = 0$   $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$   $\Rightarrow \frac{1}{2}[-2(b+1) + a(-1-1) + 4(1-b)] = 0$   $\Rightarrow -2b - 2 - 2a + 4 - 4b = 0 \Rightarrow 2a + 6b = 2$   $\Rightarrow a + 3b = 1$  ...(i) Also, given that a - b = 1 ...(ii) On solving the equations (i) and (ii), we get

a = 1, b = 0

## Question 34.

If the points P(-3,9), Q(a, b) and R(4, -5) are collinear and a + b = 1, find the value of a and b.

Solution:

Since, the points P(-3, 9), Q(a, b) and R(4, -5) are collinear, So, area of triangle  $ar(\Delta PQR) = 0$   $\frac{1}{2}[x_1(y_2-y_3) + x_2(y_3-y_1) + x_3(y_1-y_2)] = 0$   $\Rightarrow \frac{1}{2} |-3(b+5) + a(-5-9) + 4(9-b)| = 0$   $\Rightarrow -3b - 15 - 14a + 36 - 4b = 0 \Rightarrow 14a + 7b - 21 = 0$   $\Rightarrow 2a + b = 3$  ...(i) Also, given that a + b = 1 ...(ii) On solving the equations (i) and (ii), we get

a = 2, b = -1

## Question 35.

Points A(-I, y) and B(5,7) lie on a circle with centre 0(2, -3y). Find the values ofy. Hence, find the radius of the circle.

**CLICK HERE** 

🕀 www.studentbro.in

Solution:

Given, O is the centre of the circle and the points A and B lie on the circle.

OA = OB(=r)[∵ radius of same circle] So.  $OA^2 = OB^2$ ⇒ Using distance formula,  $(2+1)^{2} + (-3y-y)^{2} = (2-5)^{2} + (-3y-7)^{2}$ ⇒  $9 + 16y^2 = 9 + 9y^2 + 42y + 49$ ⇒ O (2, -3y)  $7y^2 - 42y - 49 = 0$ ⇒  $y^2 - 6y - 7 = 0$ ⇒ A (–1, y) (y-7)(y+1) = 0 $\Rightarrow$ y = -1 or 7⇒ B (5, 7) When y = -1, then co-ordinates are: O(2, 3) and A(-1, -1) Radius of circle,  $r = OA = \sqrt{(2+1)^2 + (3+1)^2} = \sqrt{9+16} = 5$  units When y = 7, then coordinates are: O(2, -21) and A(-1, 7)Radius of circle,  $r = OA = \sqrt{(2+1)^2 + (-21-7)^2} = \sqrt{9+784} = \sqrt{793}$  units.

#### Question 36.

If the point A(-I, -4); B(b, c) and C(5, -1) are collinear and 2b+c = 4, find the value of b and c. **Solution:** 

Since, the points A(-1, -4), B(b, c) and C(5, -1) are collinear, So, area of triangle, ar ( $\Delta ABC$ ) = 0  $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$   $\Rightarrow \frac{1}{2}[-1(c + 1) + b(-1 + 4) + 5(-4 - c)] = 0$   $\Rightarrow -c - 1 + 3b - 20 - 5c = 0 \Rightarrow 3b - 6c = 21$   $\Rightarrow b - 2c = 7$ ...(i) Also, given that 2b + c = 4...(ii)

Question 37.

If the point P(2, 2) is equidistant from the points A(-2, k) and B(-2k, -3), find k.

Solution:

P(2, 2)  $PA = PB \implies PA^2 = PB^2$ Since, given that Using distance formula,  $(+2+2)^{2} + (2-k)^{2} = (2+2k)^{2} + (2+3)^{2}$ ⇒  $16 + 4 - 4k + k^2 = 4 + 8k + 4k^2 + 25$ ⇒  $16 - 4k + k^2 = 8k + 4k^2 + 25$ ⇒  $3k^2 + 12k + 9 = 0$ ⇒  $k^2 + 4k + 3 = 0$ ⇒ Á(-2, k) B(-2k, -3) (k+3)(k+1) = 0⇒ k = -1 or -3⇒ When k = -1, then point A is (-2, -1)AP =  $\sqrt{(2+2)^2 + (2+1)^2} = \sqrt{16+9} = 5$  units When k = -3, then point A is (-2, -3)AP =  $\sqrt{(2+2)^2 + (2+3)^2} = \sqrt{16+25} = \sqrt{41}$  units

## Question 38.

If the point P(k - 1, 2) is equidistant from the points A(3, k) and B(k, 5), find the values of k. **Solution:** 

**CLICK HERE** 

>>

Given that point P(k-1, 2) is equidistant from the points A(3, k) and B(k, 5), so  $AP = BP \implies AP^2 = BP^2$ .**.** . Using distance formula,  $(k-1-3)^{2} + (2-k)^{2} = (k-1-k)^{2} + (2-5)^{2}$ ⇒  $(k-4)^{2} + (2-k)^{2} = (-1)^{2} + (-3)^{2}$ ⇒  $k^{2}-8k+16+4-4k+k^{2} = 1+9$ ⇒  $2k^2 - 12k + 10 = 0$ ⇒  $k^2 - 6k + 5 = 0$ ⇒  $k^2 - 5k - k + 5 = 0$ ⇒ k(k-5) - 1(k-5) = 0⇒ (k-1)(k-5) = 0⇒  $\Rightarrow$  Either k - 1 = 0 or k - 5 = 0k = 1 or 5**⇒** 

#### Question 39.

Find the ratio in which the line segment joining the points A(3, -3) and B(-2, 7) is divided by x-axis. Also find the coordinates of the point of division.

Solution:

 $A(3, -3) \xrightarrow{k \to P(x, 0)} 1 = B(-2, 7)$ 

Let point P(x, 0) on x-axis divides the join of A(3, -3) and B(-2, 7) in the ratio k : 1

Then coordinates of P are 
$$\left(\frac{-2k+3}{k+1}, \frac{7k-3}{k+1}\right)$$
  
If point P lies on x-axis, then y coordinate of P is 0.  
 $\Rightarrow \qquad \frac{7k-3}{k+1} = 0 \Rightarrow 7k-3 = 0$   
 $\Rightarrow \qquad k = \frac{3}{7}$   
 $\therefore$  Ratio is  $\frac{3}{7}$ : 1, i.e. 3: 7.  
Putting  $k = \frac{3}{7}$  in (i), we get  
the coordinates of point P =  $\left(\frac{-\frac{6}{7}+3}{\frac{3}{7}+1}, 0\right)$ , i.e.  $\left(\frac{3}{2}, 0\right)$ .

## Question 40.

Prove that the diagonals of a rectangle ABCD, with vertices A(2, -1), B(5, -1), C(5,6) and D(2,6), are equal and bisect each other.

#### Solution:

Given; A(2, -1), B(5, -1), C(5, 6) and D(2, 6) are the vertices of a rectangle ABCD. Using distance formula,

$$AC = \sqrt{(5-2)^2 + (6+1)^2} = \sqrt{9+49} = \sqrt{58} \text{ units}$$
  
BD =  $\sqrt{(5-2)^2 + (-1-6)^2} = \sqrt{9+49} = \sqrt{58} \text{ units}$   
AC = BD, i.e. diagonals are equal  
 $A(2, -1) = B(5, -1)$   
 $A(2, -1) = B(5, -1)$ 

Now, the coordinates of mid-point of AC are  $\left(\frac{2+5}{2}, \frac{6-1}{2}\right)$ , i.e.  $\left(\frac{7}{2}, \frac{5}{2}\right)$ 

The coordinates of mid-point of BD are  $\left(\frac{5+2}{2}, \frac{-1+6}{2}\right)$ , i.e.  $\left(\frac{7}{2}, \frac{5}{2}\right)$ 

As the coordinates of the mid-points of AC and BD are same, hence diagonals bisect each other.

Get More Learning Materials Here : 📕

### Question 41.

Find a point P on they-axis which is equidistant from the points A(4,8) and B(-6, 6). Also find the distance AP.

## Solution:

Let point P(0, y) on y-axis is equidistant from the points A(4, 8) and B(-6, 6).  $\therefore \qquad AP = BP \implies AP^2 = BP^2$ Using distance formula,  $\Rightarrow \qquad (4-0)^2 + (8-y)^2 = (-6-0)^2 + (6-y)^2$   $\Rightarrow \qquad 16 + 64 - 16y + y^2 = 36 + 36 - 12y + y^2$   $\Rightarrow \qquad -4y = -8 \implies y = 2$   $\therefore \text{ Point is P(0, 2)}$ Distance  $AP = \sqrt{(4-0)^2 + (8-2)^2} = \sqrt{16+36} = \sqrt{52} = 2\sqrt{13}$  units

#### Question 42.

Find the value(s) of k for which the points (3k - 1, k - 2), (k, k-1) and (k - 1, -k - 2) are collinear

## Solution:

Since the points (3k - 1, k - 2), (k, k - 7) and (k - 1, -k - 2) are collinear, so area of triangle formed by these points is zero.

$$\Rightarrow \frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
  

$$\Rightarrow \frac{1}{2}[(3k - 1)(k - 7 + k + 2) + k(-k - 2 - k + 2) + (k - 1)(k - 2 - k + 7)] = 0$$
  

$$\Rightarrow \frac{1}{2}[(3k - 1)(2k - 5) + k(-2k) + (k - 1)(5)] = 0$$
  

$$\Rightarrow \frac{1}{2}[6k^2 - 15k - 2k + 5 - 2k^2 + 5k - 5] = 0$$
  

$$\Rightarrow \frac{1}{2}[6k^2 - 15k - 2k + 5 - 2k^2 + 5k - 5] = 0$$
  

$$\Rightarrow \frac{1}{2}[4k^2 - 12k] = 0$$
  

$$\Rightarrow 2k^2 - 6k = 0$$
  

$$\Rightarrow 2k(k - 3) = 0$$
  

$$\Rightarrow k = 0 \text{ or } k - 3 = 0$$

#### Question 43.

points P, Q, R and S divide the line segment joining the points A(I, 2) and B(6, 7) in 5 equal parts. Find the coordinates of the points P, Q and R.

## Solution:

Line segment that joins points A(1, 2) and B(6, 7) is divided by points P, Q, R, S into 5 equal parts

 $\therefore \qquad AP = PQ = QR = RS = SB$ Use section formula  $\left(\frac{mx_2 + nx_1}{m + n}, \frac{my_2 + ny_1}{m + n}\right)$ P divides the join of A and B in ratio 1 : 4.  $\therefore \text{ The coordinates of P are } \left(\frac{6+4}{1+4}, \frac{7+8}{1+4}\right), \text{ i.e. P(2, 3).}$ R divides the join of A and B in the ratio 3 : 2  $\therefore \text{ The coordinates of R are } \left(\frac{18+2}{3+2}, \frac{21+4}{3+2}\right), \text{ i.e. R(4, 5).}$ Now, Q is the midpoint PR  $\therefore \text{ The coordinates of Q are } \left(\frac{12+3}{5}, \frac{14+6}{5}\right), \text{ i.e. } (3, 4)$ 

#### Question 44.

Find the value(s) of p for which the points (p + 1, 2p - 2), (p - 1, p) and (p - 6, 2p - 6) are collinear.

**CLICK HERE** 

🕀 www.studentbro.in

### Solution:

Since, the points (p + 1, 2p - 2), (p - 1, p) and (p - 3, 2p - 6) are collinear, so, area of triangle formed by these points is zero.

$$\Rightarrow \frac{1}{2}[(p+1)(p-2p+6) + (p-1)(2p-6-2p+2) + (p-3)(2p-2-p)] = 0 \Rightarrow \frac{1}{2}[(p+1)(6-p) + (p-1)(-4) + (p-3)(p-2)] = 0 \Rightarrow \frac{1}{2}[(6p-p^2 + 6-p-4p+4+p^2-2p-3p+6] = 0 \Rightarrow \frac{1}{2}[-4p+16] = 0 \Rightarrow -2p+8 = 0 \Rightarrow -2p = -8 \Rightarrow p = 4$$

## Question 45.

Find the value(s) of p for which the points (3p + 1, p), (p + 2, p - 5) and (p + 1, -p) are collinear.

#### Solution:

Since the points (3p + 1, p), (p + 2, p - 5) and (p + 1, -p) are collinear, so area of the triangle formed by these points is zero.

$$\Rightarrow \frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0 \Rightarrow \frac{1}{2}[(3p + 1) (p - 5 + p) + (p + 2) (-p - p) + (p + 1) (p - p + 5)] = 0 \Rightarrow \frac{1}{2}[(3p + 1) (2p - 5) + (p + 2) (-2p) + 5(p + 1)] = 0 \Rightarrow \frac{1}{2}[(6p^2 - 15p + 2p - 5 - 2p^2 - 4p + 5p + 5] = 0 \Rightarrow \frac{1}{2}[(4p^2 - 12p] = 0 \Rightarrow 2p^2 - 6p = 0 \Rightarrow 2p(p - 3) = 0 \Rightarrow Either p = 0 or p - 3 = 0 \Rightarrow p = 0, 3$$

#### Long Answer Type Questions [4 Marks]

#### **Question 46.**

Find the ratio in which the point P(x, 2) divides the line segment joining the points A(12,5) and B(4, -3). Also, find the value of x.

## Solution:

Let point P(x, 2) divides AB in the ratio k : 1. Using section formula, then the coordinates of P in terms of k is  $P\left(\frac{4k+12}{k+1}, \frac{-3k+5}{k+1}\right)$ P(x.2)  $\frac{-3k+5}{k+1} = 2$ A.T.Q. A(12,5) -3k + 5 = 2k + 2⇒ -5k = -3⇒  $k = \frac{3}{5}$ B(4,-3) ⇒ P(x, 2) Thus, P divides AB in the ratio 3:5 A(12,5)  $\frac{3 \times 4 + 5 \times 12}{3 + 5} = \frac{12 + 60}{8} = \frac{72}{8} = 9$ Now, x =Hence x = 9

## Question 47.

If A(-3,5), B(-2, -7), C(I, -8) and D(6,3) are the vertices of a quadrilateral ABCD, find its area. **Solution:** 

**CLICK HERE** 

🕀 www.studentbro.in

## D(6, 3) Area of quadrilateral ABCD = Area of triangle ABC + Area of triangle ACD ...(i) of triangle rate (ABC) = $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ C(1, -8) Now, $= \frac{1}{2} \left[ -3(-7+8) - 2(-8-5) + 1(5+7) \right]$ A(-3, 5) B(-2, -7) $=\frac{1}{2}[-3+26+12]=\frac{35}{2}$ sq. units ...(ii) Also, $ar(ACD) = \frac{1}{2}[-3(-8-3)+1(3-5)+6(5+8)]$ $=\frac{1}{2}[33-2+78]=\frac{109}{2}$ sq. units ...(iii) From (i), (ii), (iii), we get

ar(ABCD) = 
$$\frac{35}{2} + \frac{109}{2} = \frac{144}{2} = 72$$
 sq. units

## Question 48.

A(4, -6), B(3, -2) and C(5, 2) are the vertices of a AABC and AD is its median. Prove that the median AD divides AABC into two triangles of equal areas.

### Solution:

A(4, -6), B(3, -2) and C(5, 2) are the vertices of  $\triangle$ ABC.

 $\therefore \text{ AD is the median, so, D is the mid-point of BC.}$ ∴ Coordinates of D =  $\left(\frac{3+5}{2}, \frac{-2+2}{2}\right) = (4, 0)$ Now, ar(ABD) =  $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$ =  $\left|\frac{1}{2}[3(0+6) + 4(-6+2) + 4(-2-0)]\right|$ =  $\left|\frac{1}{2}[18 - 16 - 8]\right| = \frac{1}{2}[-6] = 3 \text{ sq. units}$ ar(ADC) =  $\left|\frac{1}{2}[4(2+6) + 5(-6-0) + 4(0-2)]\right|$ =  $\left|\frac{1}{2}[32 - 30 - 8]\right| = \frac{1}{2}[-6] = 3 \text{ sq. units}$ 

 $\therefore$  Clearly, ar(ABD) = ar(ADC).

Thus, median AD divides ∆ABC into 2 triangles of equal areas.

## Question 49.

If A(4,2), B(7,6) and C(I, 4) are the vertices of a  $\triangle$ ABC and AD is its median, prove that the median AD divides  $\triangle$ ABC into two triangles of equal areas

Solution:

Given; A(4, 2), B(7, 6) and C(1, 4) are the vertices of a triangle ABC and AD is the median.  $\therefore$  D is the mid-point of BC as AD is median A(4, 2)

$$\therefore \text{ The coordinates of D are } \left(\frac{7+1}{2}, \frac{6+4}{2}\right), \text{ i.e. } (4,5).$$
Now,  $\operatorname{ar}(ABD) = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ 

$$= \left|\frac{1}{2} [4(6-5) + 7(5-2) + 4(2-6)]\right| \xrightarrow{\mathsf{B}(7,6)} \xrightarrow{\mathsf{D}(4,5)} \xrightarrow{\mathsf{C}(1,4)}$$

$$= \left|\frac{1}{2} [4+21-16]\right| = \frac{9}{2} \text{ sq. units}$$
 $\operatorname{ar}(ADC) = \left|\frac{1}{2} [4(5-4) + 4(4-2) + 1(2-5)]\right| = \left|\frac{1}{2} [4+8-3]\right| = \frac{9}{2} \text{ sq. units}$ 

**CLICK HERE** 

🕀 www.studentbro.in

 $\therefore$  Clearly, ar(ABD) = ar(ADC).

Thus, median AD divides ∆ABC into 2 triangles of equal areas.

#### Question 50.

The mid-point P of the line segment joining the points A(- 10, 4) and B(- 2, 0) lies on the line segment joining the points C(- 9, -4) and D(- 4, y). Find the ratio in which P divides CD. Also find the value of y.

#### Solution:

 $\therefore$  P is the mid-point of the line segment joining A(-10, 4) and B(-2, 0).

$$\therefore \text{ The coordinates of P are } \left(\frac{-10-2}{2}, \frac{4+0}{2}\right), \text{ i.e. P(-6, 2).} \qquad \dots (i)$$

Let P(-6, 2) divides the join of C(-9, -4) and D(-4, y) in the ratio k : 1. Using section formula,

$$\therefore \text{ The coordinates of P are}\left(\frac{-4k-9}{k+1}, \frac{ky-4}{k+1}\right) \qquad \dots (ii)$$
  
$$\therefore \text{ From } (i), (ii)$$

A.T.Q. 
$$\frac{-4k-9}{k+1} = -6$$
 and  $\frac{ky-4}{k+1} = 2$  ...(iii)

Consider,

⇒

n ⇒ ⇒ So, P divides CD in the ratio 3:2

From (*iii*),  

$$\frac{\frac{3}{2}y-4}{\frac{3}{2}+1} = 2$$

$$\Rightarrow \qquad \frac{3y-8}{3+2} = 2 \Rightarrow 3y-8 = 10$$

$$\Rightarrow \qquad 3y = 18 \Rightarrow y = 6$$

## 2013

## Short Answer Type Questions II [3 Marks]

#### **Question 51.**

Prove that the points (7,10), (-2,5) and (3, -4) are the vertices of an isosceles right triangle. **Solution:** 

Let A (7, 10); B(-2, 5); C(3, -4) be vertices of isosceles right triangle. Now, using distance formula,

AB = 
$$\sqrt{(7+2)^2 + (10-5)^2}$$
 =  $\sqrt{81+25}$  =  $\sqrt{106}$  units  
BC =  $\sqrt{(-2-3)^2(5+4)^2}$  =  $\sqrt{25+81}$  =  $\sqrt{106}$  units  
CA =  $\sqrt{(3-7)^2 + (-4-10)^2}$  =  $\sqrt{16+196}$  =  $\sqrt{212}$  units

Clearly,

$$\therefore \qquad (\sqrt{212})^2 = (\sqrt{106})^2 + (\sqrt{106})^2$$
  

$$\Rightarrow \qquad AC^2 = AB^2 + BC^2$$
  

$$\Rightarrow \qquad \angle ABC = 90^\circ$$
  
Here, 
$$AB = BC \text{ and } \angle ABC = 90^\circ$$

So,  $\triangle ABC$  is an isosceles right triangle.

[:: Follows converse of Pythagoras theorem]

🕀 www.studentbro.in

Question 52.

Find, the ratio in which the y-axis divides the line segment joining the points (-4, -6) and (10,12). Also find the coordinates of the point of division. **Solution:** 

**CLICK HERE** 

Let point P (0, y) which lies on y-axis divides AB in the ratio k : 1. Then by section formula, in x-co-ordinates,

$$\frac{10k-4}{k+1} = 0 \implies 10k-4 = 0$$
$$k = \frac{4}{10} = \frac{2}{5}$$

Hence, point P divides AB in the ratio 2:5

Now, 
$$y = \frac{2 \times 12 - 5 \times (-6)}{2 + 5} = \frac{24 - 30}{7} = -\frac{6}{7}$$
.  
Hence, Coordinates of P are  $\left(0, \frac{-6}{7}\right)$ .



[Applying section formula for y-coordinates]

#### Question 53.

⇒

Prove that the points A(0, -1), B(-2, 3), C(6, 7) and D(8, 3) are the vertices of a rectangle ABCD?

#### Solution:

Using distance formula,

	AB = $\sqrt{(-2-0)^2 + (3+1)^2}$	$=\sqrt{4+16}$	$=\sqrt{20}$ units
	BC = $\sqrt{(6+2)^2 + (7-3)^2}$	$= \sqrt{64 + 16}$	$=\sqrt{80}$ units
	$CD = \sqrt{(8-6)^2 + (3-7)^2}$	$=\sqrt{4+16}$	$=\sqrt{20}$ units
	$DA = \sqrt{(8-0)^2 + (3+1)^2}$	$=\sqrt{64+16}$	$=\sqrt{80}$ units
Also	AC = $\sqrt{(6-0)^2 + (7+1)^2}$	$=\sqrt{36+64}$	$=\sqrt{100} = 10$ units
and	BD = $\sqrt{(8+2)^2 + (3-3)^2}$	$= \sqrt{100 + 0}$	= 10 units
Since,	AB = CD and $BC = DA$		
and diagona	dAC = BD		

In quadrilateral ABCD, opposite sides are equal and both the diagonals are equal. Therefore, ABCD is a rectangle.

#### Question 54.

Show that the points (-2,3) (8,3) and (6, 7) are the vertices of a right triangle.

#### Solution:

Using distance formula, Consider A(-2, 3), B(8, 3) and C(6, 7) Now,  $AB^2 = (8 + 2)^2 + (3 - 3)^2 = 100$  units  $BC^2 = (6 - 8)^2 + (7 - 3)^2 = 4 + 16 = 20$  units  $AC^2 = (6 + 2)^2 + (7 - 3)^2 = 64 + 16 = 80$  units Clearly, 100 = 20 + 80 $\Rightarrow AB^2 = BC^2 + AB^2$ 

So, by converse of Pythagoras theorem,  $\triangle ABC$  is a right triangle.

#### Question 55.

Prove that the points A(2, 3), B(-2, 2), C(-I, -2) and D(3, -1) are the vertices of a square ABCD.

Solution:





Using distance formula,

$$AB = \sqrt{(-2-2)^{2} + (2-3)^{2}} = \sqrt{(-4)^{2} + (-1)^{2}}$$

$$= \sqrt{16+1} = \sqrt{17} \text{ units}$$

$$BC = \sqrt{(-2+1)^{2} + (2+2)^{2}} = \sqrt{(-1)^{2} + (4)^{2}}$$

$$= \sqrt{1+16} = \sqrt{17} \text{ units}$$

$$CD = \sqrt{(-1-3)^{2} + (-2+1)^{2}} = \sqrt{(-4)^{2} + (-1)^{2}}$$

$$= \sqrt{16+1} = \sqrt{17} \text{ units}$$

$$DA = \sqrt{(3-2)^{2} + (-1-3)^{2}} = \sqrt{(1)^{2} + (-4)^{2}}$$

$$= \sqrt{1+16} = \sqrt{17} \text{ units}$$

$$Also, \quad AC = \sqrt{(-1-2)^{2} + (-2-3)^{2}} = \sqrt{(-3)^{2} + (-5)^{2}}$$

$$= \sqrt{9+25} = \sqrt{34} \text{ units}$$

$$BD = \sqrt{(-2-3)^{2} + (2+1)^{2}} = \sqrt{(-5)^{2} + (3)^{2}}$$

$$= \sqrt{25+9} = \sqrt{34} \text{ units}$$

Since, 
$$AB = BC = CD = DA$$
 and  $AC = BD$ 

 $\Rightarrow$  ABCD is a square, because all sides are equal. Diagonals are also equal.

## **Question 56.**

Find the ratio in which point P(-I, y) lying on the line segment joining points A(-3,10) and B(6, -8) divides it. Also find the value of y.

## Solution:

Let point P(-1, y) divides AB in ratio k : 1. Using sections formula for x-coordinates;

 $\frac{k : 1}{A(-3, 10) P(-1, y)} B(6, -8)$ 

÷

⇒

$$-1 = \frac{6k-3}{k+1}$$
$$k-1 = 6k-3$$
$$-7k = -2$$
$$k = \frac{2}{7}$$

Hence point P divides AB in the ratio 2:7.

Now, again using section formula for y-coordinates,

$$y = \frac{-8k+10}{k+1}$$
$$y = \frac{-8\left(\frac{2}{7}\right)+10}{\frac{2}{7}+1} = \frac{\frac{-16+70}{7}}{\frac{2+7}{7}} = \frac{70-16}{2+7} = \frac{54}{9} = 6$$

CLICK HERE

>>

R www.studentbro.in

 $\therefore$  Coordinates of P are (-1, 6).

## Question 57.

Prove that the points A(2, -1), B(3, 4), C(-2, 3) and D(-3, -2) are the vertices of a rhombus ABCD. Is ABCD a square?

Solution:

Using distance formula,

$$AB = \sqrt{(3-2)^2 + (4+1)^2} = \sqrt{(1)^2 + (5)^2} = \sqrt{1+25} = \sqrt{26} \text{ units}$$

$$BC = \sqrt{(3+2)^2 + (4-3)^2} = \sqrt{(5)^2 + (1)^2} = \sqrt{25+1} = \sqrt{26} \text{ units}$$

$$CD = \sqrt{(-2+3)^2 + (3+2)^2} = \sqrt{(1)^2 + (5)^2} = \sqrt{25+1} = \sqrt{26} \text{ units}$$

$$DA = \sqrt{(-3-2)^2 + (-2+1)^2} = \sqrt{(-5)^2 + (-1)^2} = \sqrt{25+1} = \sqrt{26} \text{ units}$$

$$AC = \sqrt{(-2-2)^2 + (3+1)^2} = \sqrt{(-4)^2 + (4)^2} = \sqrt{16+16} = \sqrt{32} \text{ units}$$

$$BD = \sqrt{(3+3)^2 + (4+2)^2} = \sqrt{(6)^2 + (6)^2} = \sqrt{36+36} = \sqrt{72} \text{ units}$$

$$B = BC = CD = DA. But AC \neq BD$$

Also,

$$\therefore AB = BC = CD = DA. But AC \neq B$$

 $\Rightarrow$  ABCD is a rhombus, not a square.

## Question 58.

Find that value of k for which the point (0, 2) is equidistant from two points (3, k) and (k, 5). Solution:



## Question 59.

If the point P(x,y) is equidistant from two points A (-3,2) and B (4, -5), prove that y = x - 2. Solution:

P(x, y)Point P(x, y) is equidistant from the points A(-3, 2) and B(4, -5). PA = PB [Given] *.*.. Using distance formula,  $\sqrt{(-3-x)^2 + (2-y)^2} = \sqrt{(4-x)^2 + (-5-y)^2}$ B(4, -5) ⇒ Squaring both sides, we get  $9 + x^{2} + 6x + 4 + y^{2} - 4y = 16 + x^{2} - 8x + 25 + y^{2} + 10y$ 6x - 4y + 13 = -8x + 10y + 41⇒ -4y - 10y = 41 - 13 - 8x - 6x⇒ -14y = -14x + 28 $\Rightarrow$ -14y = -14(x-2)⇒ y = x - 2 $\Rightarrow$ 

## **Question 60.**

The line segment AB joining the points A(3, -4), and B(I, 2) is trisected at the points P(p, -4)2) and Q(5/3, q). Find the values of p and q.

## Solution:

Now, again AP : PB = 1 : 2. Using distance formula,  

$$p = \frac{1 \times 1 + 2 \times 3}{1 + 2}$$

$$\Rightarrow p = \frac{7}{3}$$
A(3, -4)
(p, -2)
( $\frac{5}{3}$ , q)
B(1, 2)
(Also, AQ : QB = 2 : 1. Again using section formula,  

$$\Rightarrow q = \frac{2 \times 2 + 1 \times -4}{1 + 2} = 0 \Rightarrow q = 0$$

**CLICK HERE** 

>>>

## Question 61.

If the point A (x, y) is equidistant from two points P (6, -1) and Q (2,3), prove that y = x - 3. **Solution:** 

Point A(x, y) is equidistant from P(6, -1) and Q(2, 3). Using distance formula, PA = AQ

 $\Rightarrow \sqrt{(6-x)^{2} + (-1-y)^{2}} = \sqrt{(2-x)^{2} + (3-y)^{2}}$ Squaring both sides, we get  $(6-x)^{2} + (-1-y)^{2} = (2-x)^{2} + (3-y)^{2}$  $\Rightarrow 36 + x^{2} - 12x + 1 + y^{2} + 2y = 4 + x^{2} - 4x + 9 + y^{2} - 6y$  $\Rightarrow -12x + 2y + 37 = -4x - 6y + 13$  $\Rightarrow 2y + 6y = 13 - 4x + 12x - 37$  $\Rightarrow 8y = 8x - 24$  $\Rightarrow y = x - 3$ Hence, proved.

## Question 62.

If the point R (x, y) is equidistant from two points P (- 3, 4) and Q (2, -1), prove that y = x + 2.

#### Solution:

*.*..

Point R(x, y) is equidistant from the points P(-3, 4) and Q(2, -1). Using distance formula,

$$\frac{PR}{\sqrt{(x+3)^2 + (y-4)^2}} = \sqrt{(x-2)^2 + (y+1)^2}$$

Squaring both sides, we get

	$(x + 3)^{2} + (y - 4)^{2} = (x - 2)^{2} + (y + 1)^{2}$
⇒	$x^{2} + y^{2} + 6x - 8y + 9 + 16 = x^{2} + y^{2} - 4x + 2y + 4 + 1$
⇒	6x - 8y + 25 = -4x + 2y + 5
⇒	-8y - 2y = -4x - 6x + 5 - 25
⇒	-10y = -10x - 20
⇒	-10y = -10(x + 2)
⇒	y = x + 2

Hence, proved.

#### Long Answer Type Questions [4 Marks]

#### **Question 63.**

If the area of AABC formed by A(x, y), B(I, 2) and C(2, 1) is 6 square units, then prove that x +y= 15.

#### Solution:

*.*...

Point R(x, y) is equidistant from the points P(-3, 4) and Q(2, -1). Using distance formula,

**CLICK HERE** 

>>

$$PR = RQ$$

$$\sqrt{(x+3)^2 + (y-4)^2} = \sqrt{(x-2)^2 + (y+1)^2}$$

Squaring both sides, we get

 $(x + 3)^{2} + (y - 4)^{2} = (x - 2)^{2} + (y + 1)^{2}$   $\Rightarrow \quad x^{2} + y^{2} + 6x - 8y + 9 + 16 = x^{2} + y^{2} - 4x + 2y + 4 + 1$   $\Rightarrow \qquad 6x - 8y + 25 = -4x + 2y + 5$   $\Rightarrow \qquad -8y - 2y = -4x - 6x + 5 - 25$   $\Rightarrow \qquad -10y = -10x - 20$   $\Rightarrow \qquad -10y = -10(x + 2)$   $\Rightarrow \qquad y = x + 2$ 

Hence, proved.

#### Question 64.

Find the value of x for which the points (x - 1), (2,1) and (4,5) are collinear

## Solution:

Since the point A(x, -1), B(2, 1) and C(4, 5) are collinear So, area of triangle, ar( $\triangle ABC$ ) = 0

$$\Rightarrow \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0 \Rightarrow \frac{1}{2} |x(1 - 5) + 2(5 + 1) + 4(-1, -1)| = 0 \Rightarrow |-4x + 12 - 8| = 0 \Rightarrow |-4x + 4| = 0 \Rightarrow -4x + 4 = 0 \Rightarrow 4x = 4 \Rightarrow x = 1$$

## Question 65.

The three vertices of a parallelogram ABCD are A(3, -4), B(-I, -3) and C(-6, 2). Find the coordinates of vertex D and find the area of parallelogram ABCD.

D(x, y)

A(3, -4)

C(-6, 2)

B(-1, -3)

## Solution:

Given ABCD is a parallelogram Let coordinates of point D be (x, y).

The coordinates of mid-point of AC =  $\left(\frac{-6+3}{2}, \frac{2-4}{2}\right) = \left(\frac{-3}{2}, -1\right)$ 

The coordinates of mid-point of BD =  $\left(\frac{x-1}{2}, \frac{y-3}{2}\right)$ 

Since, diagonals of a parallelogram bisect each other, so, P is the mid-point of AC as well as BD.

$$\Rightarrow \qquad \left(\frac{x-1}{2}, \frac{y-3}{2}\right) = \left(\frac{-3}{2}, -1\right)$$

Comparing both sides, we get

$$\Rightarrow \frac{x-1}{2} = \frac{-3}{2} \text{ and } \frac{y-3}{2} = -1$$

$$\Rightarrow x-1 = -3 \text{ and } y-3 = -2$$

$$\Rightarrow x = -2 \text{ and } y = 1$$
Therefore, coordinates of D are (-2, 1).
Now,  $\operatorname{ar}(\Delta ABC) = \frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ 

$$= \frac{1}{2} |3(-3-2) - 1(2+4) - 6(-4+3)|$$

$$= \frac{1}{2} |-15 - 6 + 6| = \frac{15}{2} \text{ sq. units}$$
Area of parallelogram(ABCD) = 2 ar ( $\Delta ABC$ )
$$= 2 \times \frac{15}{2} = 15 \text{ sq. units}$$

## **Question 66.**

If the points A(I, -2), B(2,3), C(-3,2) and D(-4, -3) are the vertices of parallelogram ABCD, then taking AB as the base, find the height of this parallelogram **Solution:** 

CLICK HERE

>>

Using distance formula,

AB = 
$$\sqrt{(2-1)^2 + (3-(-2))^2} = \sqrt{26}$$
 units  
Area  $\triangle ABC$  =  $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$   
=  $\frac{1}{2}|1(3-2) + 2\{2-(-2)\} + (-3)(-2-3)|$   
=  $\frac{1}{2} \times 24 = 12$  sq. units  
 $\therefore$  Area of ||gm ABCD = 2 × area of  $\triangle ABC$  D(-4, -3) C(-3, 2)  
=  $2 \times 12 = 24$  sq. units  
Now, area ||gm ABCD = Base × h [ $\because$  By formula]  
=  $AB \times h$   
 $\Rightarrow$   $AB \times h = 24$   
 $\Rightarrow$   $h = \frac{24}{\sqrt{26}}$   
 $\Rightarrow$   $h = \frac{24}{26} \times \sqrt{26}$   
 $\Rightarrow$  Height of parallelogram =  $\frac{12}{13}\sqrt{26}$  units

## Question 67.

For the AABC formed by the points A(4, -6), B(3, -2) and C(5,2), verify that median divides the triangle into two triangles of equal area.

#### Solution:

Consider AD is median of  $\triangle ABC$ .

Here D is mid point of BC as AD is median

 $\therefore \text{ Coordinate of D are } x = \frac{3+5}{2} = 4$   $y = \frac{-2+2}{2} = 0$ Coordinates of D are (4, 0). Now Area of  $\triangle ABD = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$   $= \frac{1}{2} [4(0+2) + 4(-2+6) + 3(-6-0)]$   $= \frac{1}{2} [8 + 16 - 18] = \left|\frac{6}{2}\right| = 3 \text{ sq. units}$ Now, Area of  $\triangle ACD = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$   $= \frac{1}{2} [4(0-2) + 4(2+6) + 5(-6-0)]$   $= \frac{1}{2} [-8 - 32 - 30] = \frac{1}{2} [32 - 38] = \frac{1}{2} [-6] = 3 \text{ sq. units}$ 



Clearly, ar  $\triangle ABD = ar \triangle ACD$ . Thus, median AD divides triangle in q triangles of equal area.

Get More Learning Materials Here :

CLICK HERE

#### Question 68.

Find the area of a parallelogram ABCD if three of its vertices are A(2, 4), B(2 +  $\sqrt{3}$ ,5) and C(2, 6).

Solution:

ABCD is a parallelogram, A(2, 4), B(2 +  $\sqrt{3}$ , 5), C(2, 6) form the vertices of  $\triangle$ ABC.



Diagonal AC divides the parallelogram in two triangles of equal area.  $\therefore$  Area of parallelogram ABCD = 2(Area of  $\triangle$ ABC) = 2( $\sqrt{3}$ ) = 2 $\sqrt{3}$  sq. units.

#### **Question 69.**

If the area of the triangle formed by points A (x,y), B (1,2) and C (2,1) is 6 square units, then show that x + y = 15.

#### Solution:

The points are A(x, y), B(1, 2) and C(2, 1) Area of  $\triangle ABC = \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| = 6$  sq. units [Given]  $\Rightarrow \qquad \frac{1}{2} |x(2-1) + 1(1-y) + 2(y-2)| = 6$   $\Rightarrow \qquad |x + 1 - y + 2y - 4| = 12$   $\Rightarrow \qquad |x + y - 3| = 12$   $\Rightarrow \qquad x + y - 3 = 12$  $\Rightarrow \qquad x + y = 15$ 

Hence, proved.

## Question 70.

Find the area of the triangle formed by joining the mid-points of the sides of a triangle whose vertices are (3,2), (5,4) and (3, 6).

#### Solution:

Consider, the points are A(3, 2), B(5, 4) and C(3, 6) form the vertices of  $\triangle ABC$ .

Let D, E and F be the mid-points of the sides AB, BC and AC respectively of the triangle ABC.

 $\therefore \text{ Coordinates of D are } \left(\frac{3+5}{2}, \frac{2+4}{2}\right), \text{ i.e. the coordinates of D are } (4, 3) \xrightarrow{\mathsf{A}(3, 2)} \left(\begin{array}{c} \mathsf{A}(3, 2) \\ \mathsf{Coordinates of E are } \left(\frac{5+3}{2}, \frac{4+6}{2}\right) \\ \Rightarrow \text{ Coordinates of E = } (4, 5) \\ \text{ Coordinates of F are } \left(\frac{3+3}{2}, \frac{6+2}{2}\right) \\ \Rightarrow \text{ Coordinates of F are } (3, 4). \\ \text{ Coordinates of D(4, 3), E(4, 5), F(3, 4)} \end{array}\right)$ 

Now, Area of triangle = 
$$\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
Area of  $\Delta DEF = \frac{1}{2}[4(5-4) + 4(4-3) + 3(3-5)] = \frac{2}{2} = 1$  sq. unit

#### Question 71.

If the area of the triangle formed by joining the points A (x, y), B (3, 2) and C (- 2, 4) is 10 square units, then show that 2x + 5y + 4 = 0. Solution:

**CLICK HERE** 

We know that,

Area of 
$$\triangle ABC = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 10$$
 sq. units  

$$= \frac{1}{2} |x(2 - 4) + (3) (4 - y) - 2(y - 2)| = 10$$
 sq. units  

$$20 = (-2x - 5y + 16)$$
  

$$-2x - 5y + 16 - 20 = 0$$
  

$$\Rightarrow 2x + 5y + 4 = 0$$
 Hence proved  

$$B(3, 2) = C(-2, 4)$$

#### 2010

#### Very Short Answer Type Questions [1 Mark]

#### Question 72.

If a point A(0, 2) is equidistant from the points B(3, p) and C(p, 5), then find the value of p. **Solution:** 

Given points are A(0, 2), B(3,p), C(p, 5)According to question,

$$AB = AC$$

Using distance formula

$$\sqrt{(3-0)^2 + (p-2)^2} = \sqrt{(p-0)^2 + (5-2)^2}$$
  
Squaring both sides  
$$9 + p^2 + 4 - 4p = p^2 + 9$$
$$4 - 4p = 0$$
$$p = 1$$

#### Question 73.

Find the value of k, if the point P(2,4) is equidistant from the points A(5, k) and B(k, 7).

Solution:



## Question 74.

*.*:.

Find the ratio in which the line segment joining the points (1,-3) and (4,5) is divided by x-axis. **Solution:** 

Let the ratio in which the line segment joining (1, -3) and (4, 5) is divided by x-axis be k : 1Therefore, the coordinates of the point of division is  $\left(\frac{4k+1}{k+1}, \frac{5k-3}{k+1}\right)$ 

**CLICK HERE** 

[∵ Using section formula]

🕀 www.studentbro.in

We know that y-coordinate of any point on x-axis is 0.

 $\frac{5k-3}{k+1} = 0$  5k-3 = 0 5k = 3  $k = \frac{3}{5}$ Ratio = k: 1 = 3: 5

Short Answer Type Questions II [3 Marks]

## **Question 75.**

If the vertices of a triangle are (1, -3) (4,p) and (-9,7) and its area is 15 sq. units, find the value(s) of p.

#### Solution:

Let the triangle be ABC with vertices A(1, -3), B(4, p), C(-9, 7). A(1, -3) Area of  $\triangle ABC = 15$  sq. units.  $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 15$  $\frac{1}{2}[1(p-7) + 4(7+3) - 9(-3-p)] = 15$ p - 7 + 40 + 27 + 9p = 30B(4, p)

p = -3



#### **Question 76.**

A point P divides the line segment joining the points A(3, -5) and B(-4, 8) such AP/PB=k/1. If P lies on the line x + y = 0, then find the value of K.

## Solution:

AB is a line with A(3, -5) and B(-4, 8). P(x, y) is any point on AB such that AP : PB = K : 1. Using section formula

$$(x, y) = \left(\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2}\right) \xrightarrow{A(3, -5)} \xrightarrow{P(x, y)} \xrightarrow{B(-4, 8)}$$

Here,

$$x_1 = 3, \quad x_2 = -4, \quad y_1 = -5, y_2 = 8, \quad m_1 = K, \quad m_2 = 1.$$
  
 $(x, y) = \left(\frac{K(-4) + 1(3)}{K+1}, \frac{K(8) + 1(-5)}{K+1}\right)$ 

x + y = 0

$$(x, y) = \left(\frac{-4K+3}{K+1}, \frac{8K-5}{K+1}\right)$$

On equating the coordinates both sides, we get

$$x = \frac{-4K+3}{K+1}, \quad y = \frac{8K-5}{K+1}$$

Given that,

$$\frac{-4K+3}{K+1} + \frac{8K-5}{K+1} = 0$$

$$\frac{-4K+3+8K-5}{K+1} = 0$$

$$4K-2 = 0$$

$$4K = 2$$

$$K = \frac{2}{4} =$$

$$K = \frac{1}{2}.$$

## Question 77.

Find the coordinates of a point P, which lies on the line segment joining the points A(-2, -2) and B(2, -4) such that AP = 3/7 AB. Solution:

CLICK HERE

>>

🕀 www.studentbro.in

1  $\overline{2}$  Given that,

$$AP = \frac{3}{7}AB \implies \frac{AP}{AB} = \frac{3}{7} \implies AP: PB = 3:4$$

$$AP = \frac{3}{7}AB \implies \frac{4}{1}$$

Using section formula,

$$x = \frac{3(2) + 4(-2)}{3+4} = \frac{6-8}{7} = -\frac{2}{7}$$
$$y = \frac{3(-4) + 4(-2)}{3+4} = \frac{-12-8}{7} = \frac{-20}{7}$$

Coordinates of P are  $\left(\frac{-2}{7}, \frac{-20}{7}\right)$ 

### Question 78.

Find the area of the quadrilateral ABCD whose vertices are A(-3, -1), B(-2, -4), C(4, -1) and D(3, 4).

## Solution:

Area of quadrilateral ABCD = Area of  $\triangle ABC$  + Area of  $\triangle ACD$ 

where area of triangle is  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ 

$$= \frac{1}{2}[-3(-4+1) + (-2)(-1+1) + 4(-1+4)]$$

$$+ \frac{1}{2}[-3(-1-4) + 4(4+1) + 3(-1+1)]$$

$$= \frac{1}{2}[-3(-3) + (-2)(0) + 4(3)] + \frac{1}{2}[-3(-5) + 4(5) + 3(0)]$$

$$= \frac{1}{2}[9+0+12] + \frac{1}{2}[15+20] = \frac{1}{2} \times 21 + \frac{1}{2} \times 35$$

$$A(-3,-1)$$

$$B(-2,-4)$$

$$= \frac{1}{2} \times 56 = 28$$
 Sq. units.

## Question 79.

If the points A(x, y), B(3, 6) and C(-3,4) are collinear, show that x - 3y + 15 = 0. Solution: If A, B and C are collinear then area of  $\triangle ABC = 0$ 

$$\Rightarrow \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) = 0 \quad A(x, y) \qquad B(3, 6) \qquad C(-3, 4)$$
  

$$\Rightarrow \frac{1}{2} [x(6-4) + 3(4-y) + (-3)(y-6)] = 0$$
  

$$\Rightarrow \qquad 2x + 12 - 3y - 3y + 18 = 0$$
  

$$\Rightarrow \qquad 2x - 6y + 30 = 0$$
  

$$\Rightarrow \qquad x - 3y + 15 = 0$$

Hence, proved.

## **Question 80.**

Find the value of £, for which the points A(6, -1), B(& – 6) and C(0, -7) are collinear. **Solution:** 



Given points are A(6, -1), B(k, -6), C(0, -7).  
As A, B, C are collinear points, so, Ar 
$$\triangle ABC = 0$$
  

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
i.e.,  $\frac{1}{2} [6(-6+7) + k(-7+1) + 0(-1+6)] = 0$   
 $\frac{1}{2} [6-6k+0] = 0$   
 $\frac{1}{2} [6-6k] = 0$   
 $[6-6k] = 0$   
 $6-6k = 0$   
 $6(1-k) = 0$   
 $1-k = 0$   
 $k = 1.$ 

C(0, -7)

## Question 81.

Find the value of p, if the points A(I, 2), B(3,p) and C(5, -4) are collinear. **Solution:** 

If three points are collinear, then area bounded by them is zero.

i.e.,  

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$\frac{1}{2} [1(p+4) + 3(-4-2) + 5(2-p)] = 0$$

$$\frac{1}{2} [p+4-18+10-5p] = 0$$

$$\frac{1}{2} [p+4-18+10-5p] = 0$$

$$\frac{1-4p-4}{4p+4} = 0$$

$$p = -1$$

## Question 82.

Find the area of the triangle whose vertices are (-7, -3), (1, -7) and (3,0). **Solution:** 

The area of the  $\Delta = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ Here,  $x_1 = -7, \quad x_2 = 1, \quad x_3 = 3$   $y_1 = -3, \quad y_2 = -7, \quad y_3 = 0$ Area of the triangle  $= \frac{1}{2} [-7(-7-0) + 1 \{0 - (-3)\} + 3 \{-3 - (-7)\}]$   $= \frac{1}{2} [(-7)(-7) + (1)(3) + 3(-3 + 7)]$   $= \frac{1}{2} [49 + 3 + (3 \times 4)]$  $= \frac{1}{2} [49 + 3 + 12] = \frac{1}{2} \times 64 = 32$  sq. units.

## Question 83.

Find the ratio in which the y-axis divides the line segment joining the points (5, -6) and (-1, -4). Also find the coordinates of the point of intersection. **Solution:** 

CLICK HERE

>>>

Let the ratio be K : 1. Then by the section formula, the coordinates of the point which divides the line segment in the ratio K : 1 are  $\left(\frac{-K+5}{K+1}, \frac{-4K-6}{K+1}\right)$  [:: Using section formula]

This point lies on the y-axis and we know that on the y-axis, x is 0.

$$\therefore \qquad \frac{-K+5}{K+1} = 0 \qquad \xrightarrow{K : 1}_{A(5,-6)} P(x, y) \qquad B(-1, -4)$$
  
-K + 5 = 0  
K = 5

The ratio is 5:1.

On putting the value of K = 5, we get the point of intersection 
$$\left(\frac{-5+5}{5+1}, \frac{-4\times5-6}{5+1}\right)$$

$$\Rightarrow \qquad \left(0, -\frac{-3}{6}\right)$$
$$\Rightarrow \qquad \left(0, \frac{-13}{3}\right)$$

 $\therefore$  coordinates of point of intersection are  $\left(0, \frac{-13}{3}\right)$ 

#### **Question 84.**

Find the value of y for which the points (5, -4), (3, -1) and (1, y) are collinear. **Solution:** 

The points are collinear so area of triangle = 0

So,  
Area of triangle = 
$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
Here,  
 $x_1 = 5, x_2 = 3, x_3 = 1$   
 $y_1 = -4, y_2 = -1, y_3 = y$   
Area of triangle =  $\frac{1}{2} [5(-1-y) + 3(y+4) + 1(-4+1)]$   
 $= \frac{1}{2} [-5-5y+3y+12-3]$   
 $= \frac{1}{2} [-5y+3y-5+9]$   
 $= \frac{1}{2} [-2y+4] = \frac{1}{2} \times 2(-y+2) = (-y+2)$   
As per condition area of triangle must be zero

As per condition, area of triangle must be zero. -y + 2 = 0

$$+2 = 0$$
  
 $-y = -2$   
 $y = 2$ 

#### Question 85.

For what value of k, (k > 0), is the area of the triangle with vertices (-2, 5), (k, -4) and  $\{2k + 1,10\}$  equal to 53 sq. units? Solution:



Vertices of the triangle are (-2, 5), (k, -4) and (2k + 1, 10). Then, Ar(Triangle) = 53 sq. units  $\Rightarrow \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 53$  $\frac{1}{2} \left| -2\left(-4 - 10\right) + k\left(10 - 5\right) + \left(2k + 1\right)\left(5 - \left(-4\right)\right) \right| = 53$ ⇒ |28 + 5k + 18k + 9| = 106⇒  $|23k + 37| = 106 \implies 23k + 37 = \pm 106$ ⇒ 23k + 37 = 106 or 23k + 37 = -106⇒ 23k = 69 or 23k = -143 $\Rightarrow$ k = 3 or  $k = \frac{-143}{23}$ ••• Given, k > 0 ... k = 3

## **2011**

#### Short Answer Type Questions I [2 Marks]

## Question 86.

Find that value(s) of x for which the distance between the points P(JC, 4) and Q(9,10) is 10 units.

#### Solution:

Given that,	PQ = 10 units	0(9, 10)
⇒	$PQ^2 = 100$	Gle
Using distance	e formula, $P(x, 4)$	to units
⇒	$(x-9)^2 + (4-10)^2 = 100$	10 0.00
$\Rightarrow$	$(x-9)^2 + 36 = 100$	
⇒	$(x-9)^2 = 64$	
⇒	$x-9 = \pm 8$	
$\Rightarrow$	x - 9 = 8 or $x - 9 = -8$	
$\Rightarrow$	x = 17 or $x = 1$ .	

## Question 87.

Find the point ony-axis which is equidistant from the points (-5, -2) and (3, 2).

#### Solution:

Let point P(0, y) on y-axis be equidistant from A(-5, -2) and B(3, 2). So, PA = PB PA<sup>2</sup> = PB<sup>2</sup> Using distance formula,  $\Rightarrow 5^{2} + (y + 2)^{2} = (-3)^{2} + (y - 2)^{2}$   $\Rightarrow 25 + y^{2} + 4y + 4 = 9 + y^{2} - 4y + 4$   $\Rightarrow 8y = -16 \Rightarrow y = -2$ Hence, required points is (0, -2)

## Question 88. .

If P(2,4) is equidistant from Q(7, 0) and R(x, 9), find the values of x. Also find the distance PQ.

CLICK HERE

>>

🕀 www.studentbro.in

Solution:



## Question 89.

Find the value of k, if the points P(5,4), Q(7, k) and R(9, -2) are collinear

## Solution:

Since points P, Q, R are collinear.

	• e -e			
So,	area of $\Delta PQR = 0$	P(5, 4)	Q(7, k)	R(9,2)
⇒	$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$			
⇒	$\frac{1}{2}[5(k+2) + 7(-2-4) + 9(4-k)] = 0$			
⇒	$\frac{1}{2}[5k + 10 - 42 + 36 - 9k] = 0$			
⇒	-4k+4 = 0			
⇒	$4k = 4 \implies k$	: = 1		

## Question 90.

If (3, 3), (6, y), (x, 7) and (5, 6) are the vertices of a parallelogram taken in order, find the values of x and y.

#### Solution:

D(5, 6) ABCD is a ||gm, [Given] C(x, 7) P is the mid-point of AC and BD. [: Property of parallelogram] Taking AC, Coordinates of point P is  $\left(\frac{x+3}{2}, 5\right)$ [∵ Using mid-point formula] A(3, 3) B(6, y) Taking BD, Also, coordinates of point P is  $\left(\frac{11}{2}, \frac{y+6}{2}\right)$ [:: Using mid-point formula]  $\frac{x+3}{2} = \frac{11}{2}$  and  $\frac{y+6}{2} = 5$  [:: As P is mid-point of AC & BD] A.T.Q x + 3 = 11y + 6 = 10x = 8y = 4

## Question 91.

If two vertices of an equilateral triangle are (3,0) and (6,0), find the third vertex. **Solution:** 



Let ABC be an equilateral  $\Delta$ . A(x, y)Let coordinates of points A, B and C are (x, y), (3, 0) and (6, 0)respectively. Now AB = AC = BC[: In equilateral  $\Delta$ , all sides are equal]  $AB^2 = AC^2 = BC^2$ C(6, 0) B(3, 0)  $\Rightarrow$ Using distance formula,  $(x-3)^2 + y^2 = (x-6)^2 + y^2 = 3^2$ ⇒  $(x-3)^2 + y^2 = (x-6)^2 + y^2$  ...(i) and  $(x-3)^2 + y^2 = 3^2$ ⇒ ...(ii) Solving (i);  $(x-3)^2 = (x-6)^2$ ⇒  $x^2 - 6x + 9 = x^2 - 12x + 36$ ⇒ 6x = 27 $\Rightarrow$  $x = \frac{27}{6} = \frac{9}{2}$ -Put  $x = \frac{9}{2}$  in eqn (*ii*) we get  $\left(\frac{9}{2} - 3\right)^2 + y^2 = 3^2$  $\left(\frac{3}{2}\right)^2 + y^2 = 3^2$ ⇒  $\frac{9}{4} + y^2 = 9$ ⇒  $y^2 = 9 - \frac{9}{4} = \frac{27}{4} \implies y = \frac{3\sqrt{3}}{2}$ ⇒ Hence, the third vertex is  $\left(\frac{9}{2}, \frac{3\sqrt{3}}{2}\right)$ 

## Question 92.

Point M(11,y) lies on the line segment joining the points P(15,5) and Q(9,20). Find the ratio in which point M divides the line segment PQ. Also find the value ofy

#### Solution:

Let point M divides the line segment PQ in the ratio k: 1

Then, Using section formula to calculate coordinates of M, and equating with given M-coordinates.  $\bigcirc Q(9, 20)$ 

$$\frac{9k+15}{k+1} = 11 \text{ and } \frac{20k+5}{k+1} = y \dots(i)$$

$$\Rightarrow \qquad 9k+15 = 11k+11$$

$$\Rightarrow \qquad 2k = 4 \Rightarrow k = 2 \qquad P(15,5)$$

Hence, point M divides the line segment PQ in the ratio 2 : 1. Then, using (i),

$$y = \frac{20 \times 2 + 5}{2 + 1} = \frac{45}{3} = 15$$
  
$$y = 15$$

#### Question 93.

*:*..

⇒

The point A(3,y) is equidistant from the points P(6,5) and Q(0, -3). Find the value of y.

 $16y = 16 \implies y = 1$ 

**CLICK HERE** 

>>

Solution:  
Given:  

$$AQ = AP$$
  
 $\Rightarrow$   
 $Q^2 = AP^2$   
Using distance formula,  
 $\Rightarrow$   
 $(3-0)^2 + (y+3)^2 = (3-6)^2 + (y-5)^2$   
 $\Rightarrow$   
 $9 + y^2 + 6y + 9 = 9 + y^2 - 10y + 25$   
 $\Rightarrow$   
 $(6, 5)$   
 $P(6, 5)$ 

R www.studentbro.in

Q(0, -3)

## Question 94.

Point P(x, 4) lies on the line segment joining the points A(-5,8) and B(4, -10). Fmd the ratio in which point P divides the line segment AB. Also find the value of x

## Solution:

Let point P divides the line segment AB in the ratio 
$$k : 1$$
  
Using distance formula  
A.T.Q.,  

$$\frac{4k-5}{k+1} = x \text{ and } \frac{-10k+8}{k+1} = 4$$

$$\Rightarrow -10k+8 = 4k+4$$

$$14k = 4$$

$$k = \frac{4}{14} = \frac{2}{7}$$

$$k = \frac{2}{7}$$

So, point P divides the line segment AB in the ratio 2:7

$$x = \frac{4 \cdot \left(\frac{2}{7}\right) - 5}{\frac{2}{7} + 1} = \frac{8 - 35}{2 + 7} = \frac{-27}{9} = -3$$
$$x = 3$$

121

#### Question 95.

Now,

Find the area of the quadrilateral ABCD, whose vertices are A(-3, -1), B(-2, -4), C(4, -1) and D(3, 4).

Solution:

Firstly,



## Question 96.

Now,

Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are A(2,1), B(4,3) and C(2,5). **Solution:** 

CLICK HERE

>>

🕀 www.studentbro.in

D, E, F are the mid-points of the sides BC, CA and AB respectively.
 So, coordinates of the points D, E, F are as Using mid-point formula,

 $D\left(\frac{4+2}{2}, \frac{3+5}{2}\right); E\left(\frac{2+2}{2}, \frac{5+1}{2}\right); F\left(\frac{4+2}{2}, \frac{3+1}{2}\right)$ i.e. D(3, 4); E(2, 3); F(3, 2) Now, ar( $\Delta DEF$ ) =  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$ =  $\frac{1}{2} [3(3-2) + 2(2-4) + 3(4-3)]$ =  $\frac{1}{2} [3-4+3] = \frac{2}{2} = 1$  sq. unit

C(2, 5)

#### Question 97.

Find the value of y for which the distance between the points A(3, -1) and B(11,y) is 10 units. **Solution:** 

Given that:	AB =	10 unit	s	B(11, Y)
$\Rightarrow$	$AB^2 =$	100		B(III)
Using distan	ce formula,		A(3,-1) 10	
⇒	$(11-3)^2 + (y+1)^2 =$	100		
⇒	$64 + (y + 1)^2 =$	100		
⇒	$(y+1)^2 =$	36		
⇒	y + 1 =	<b>±</b> 6		
⇒	y + 1 =	6 or	y + 1 = -6	
⇒	<i>y</i> =	5 or	y = -7.	

#### Question 98.

Find a relation between jt and y such that the point P(x, y) is equidistant from the points A(1, 4) and B(-1, 2).

Solution:



**CLICK HERE** 

>>

🕀 www.studentbro.in

## Question 99.

Find a point on x-axis which is equidistant from A(4, -3) and B(0,11). Solution:



Hence, coordinates of required point are (-12, 0)

#### Question 100.

If A(-2,3), B(6,5), C(x, -5) and D(-4, -3) are the vertices of a quadrilateral ABCD of area 80 sq. units, then find positive value of x.

#### Solution:

ar (quad ABCD) = ar ( $\triangle$ ABD) + ar ( $\triangle$ BCD)  $80 = \left|\frac{1}{2}\left[-2(5+3)+6(-3-3)-4(3-5)\right]\right| + \left|\frac{1}{2}\left[6(-5+3)+x(-3-5)-4(5+5)\right]\right|$ [: Area of triangle =  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$  $80 = \left|\frac{1}{2}\left[-16 - 36 + 8\right]\right| + \left|\frac{1}{2}\left[-12 - 8x - 40\right]\right|$ ⇒  $80 = \left|\frac{1}{2}(-44)\right| + \left|\frac{1}{2}(-8x - 52)\right|$ D(-4, -3) -5)  $\Rightarrow$ 80 = 22 + |26 + 4x|⇒  $|26x + 4x| = 58 \Rightarrow 26 + 4x = \pm 58$  $\Rightarrow$  $[\because |x| = a \Rightarrow x = \pm a]$ 26 + 4x = 58 or 26 + 4x = -58⇒ A(-2.3) B(6, 5) 4x = 32 or 4x = -84⇒ x = 8 or x = -21  $\therefore$  Positive value of x = 8 $\Rightarrow$ 

#### Question 101.

Find the area of the quadrilateral PQRS whose vertices are P(-I, -3), Q(5, -7), R(10, -2) and S(5,17).

#### Solution:

ar (quad PQRS) = ar (
$$\Delta$$
PQR) + ar ( $\Delta$ PRS)  
=  $\frac{1}{2} [-1(-7+2)+5(-2+3)+10(-3+7)] + \frac{1}{2} [-1(-2-17)+10(17+3)+5(-3+2)]$   
[:: Area of triangle =  $\frac{1}{2} [x_1(y_2-y_3)+x_2(y_3-y_1)+x_3(y_1-y_2)]]$ 

$$= \frac{1}{2}[5+5+40] + \frac{1}{2}[19+200-5]$$
  
= 25 + 107 = 132 sq. units.



🕀 www.studentbro.in

#### Question 102.

Find the area of the quadrilateral ABCD whose vertices are A(3, -1), B(9, -5), C(14,0) and D(9,19). Solution:

**CLICK HERE** 

>>

Firstly, ar 
$$(\Delta ABC) = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  

$$= \frac{1}{2} [3(-5-0) + 9(0+1) + 14(-1+5)]$$

$$= \frac{1}{2} [-15+9+56]$$

$$= \frac{1}{2} \times 50 = 25 \text{ sq. units.}$$
A(3, -1)
B(9, -5)
Now, ar  $(\Delta ACD) = \frac{1}{2} [3(0-19) + 14(19+1) + 9(-1-0)]$ 

$$= \frac{1}{2} [-57+280-9]$$

$$= \frac{1}{2} \times 214 = 107 \text{ sq. units.}$$
Area of quadrilateral ABCD = ar( $\Delta ABC$ ) + ar( $\Delta ACD$ ) = 25 + 107 = 132 sq. units

#### Question 103.

Find the coordinates of the points which divide the line segment joining A (2, -3) and B(-4, -6) into three equal parts.

#### Solution:

Let P and Q are the required point; which divides AB in three equal parts.



## 2010

## Very Short Answer Type Questions [1 Mark]

#### Question 104.

If P(2, p) is the mid-point of the line segment joining the points A(6, -5) and B(-2,11), find the value of p.

#### Solution:

P(2, p) is mid-point of A (6, -5) and B (-2,11). Using mid-point formula,

⇒

$$\frac{-5+11}{2} = p$$
$$p = \frac{6}{2} \Rightarrow p = 3.$$

## Question 105.

If A(I, 2), B(4, 3) and  $\in$ (6,6) are three vertices of parallelogram ABCD, find co-ordinates of D. **Solution:** 

CLICK HERE

>>>

Let coordinates of D be (x, y) and P is mid-point of AC and BD. [Diagonals of a parallelogram bisect each other]

.: Using mid-point formula,

$\left(\frac{x+4}{2}, \frac{y+3}{2}\right) = \left(\frac{1+6}{2}, \frac{2+6}{2}\right)$
$\frac{x+4}{2} = \frac{7}{2}, \frac{y+3}{2} = \frac{8}{2}$
x + 4 = 7; y + 3 = 8
x = 3; y = 5

Coordinates of D are (3, 5). *.*..

#### Question 106.

What is the distance between the points A(c, 0) and B(0, -c)?

## Solution:

⇒

⇒ ⇒

Distance

AB = 
$$\sqrt{(0-c)^2 + (-c-0)^2}$$
 [:: Using distance formula]  
=  $\sqrt{c^2 + c^2} = \sqrt{2c^2} = \sqrt{2c}$  units

D (x, y)

A (1, 2)

C (6,6)

B (4, 3)

#### Question 107.

Find the distance between the points, A(2a, 6a) and B(2a +  $\sqrt{3}$  a, 5a).

## Solution:

Distance

AB = 
$$\sqrt{(2a + \sqrt{3a} - 2a)^2 + (5a - 6a)^2}$$
 [:: Using distance formula]  
=  $\sqrt{3a^2 + a^2} = \sqrt{4a^2} = 2a$  units

## Question 108.

Find the value of k if P(4, -2) is the mid point of the line segment joining the points A(5k, 3) and B(-k, -7).

## Solution:

P(4, -2) is mid point of A(5k, 3) and B(-k, -7), Using mid-point formula,  $\frac{5k-k}{2} = 4 \implies 4k = 8 \implies k = 2$ *.*..

#### Short Answer Type Questions II [3 Marks]

### Question 109.

Point P divides the line segment joining the points A(2,1) and B(5, -8) such that AP /AB=1/3. If P lies on the line 2x - y + k = 0, find the value of k. Solution:







P is the point of intersection of line segment AB and line 2x - y + k = 0.

Here, given that,	$\frac{AP}{AB} = \frac{1}{3} \implies 3AP = AB$
⇒	3AP = AP + PB
⇒	2AP = PB
⇒	$\frac{AP}{PB} = \frac{1}{2} \Rightarrow AP : PB = 1 : 2$

 $\Rightarrow$  P divides the line segment joining A(2, 1) and B(5, -8) in the ratio 1:2.

.: Coordinates of point P are

$$x = \frac{1 \times 5 + 2 \times 2}{1 + 2} = 3 \quad [\because \text{ Using section formula}]$$
$$y = \frac{1 \times (-8) + 2 \times 1}{1 + 2} = -2$$

i.e. P (3, -2)

As point P lies on the line 2x - y + k = 0, P must satisfy it.  $\Rightarrow \qquad 6 + 2 + k = 0 \Rightarrow k = -8$ 



#### Question 110.

If R(x, y) is a point on the line segment joining the points P(a, b) and Q(b, a), then prove that x + y = a + b.

### Solution:

R(x, y) lies on the line segment joining the points P(a, b) and Q(b, a). Then P, Q, R are collinear, so  $ar(\Delta PQR) = 0$ 

$$\Rightarrow \frac{1}{2} |x(b-a) + a(a-y) + b(y-b)| = 0 \begin{bmatrix} \text{Using formula for area of a triangle} \\ \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] \end{bmatrix}$$
  

$$\Rightarrow bx - ax + a^2 - ay + by - b^2 = 0$$
  

$$\Rightarrow b(x + y) - a(x + y) + (a^2 - b^2) = 0$$
  

$$\Rightarrow (b-a) (x + y) - (b-a) (b + a) = 0$$
  

$$\Rightarrow (b-a) [(x + y) - (b + a)] = 0$$
  

$$\Rightarrow x + y = b + a$$
  
[Assuming  $a \neq b$ ] Hence, proved.

## Question 111.

Prove that the points P(a, b + c), Q(b, c + a) and R(c, a + b) are collinear.

## Solution:

Area of  $\Delta$  formed by the points P(a, b + c), Q(b, c + a) and R(c, a + b) is given by

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$
  
or, 
$$ar(\Delta PQR) = \frac{1}{2} |a(c + a - a - b) + b(a + b - b - c) + c(b + c - c - a)|$$
$$= \frac{1}{2} |a(c - b) + b(a - c) + c(b - a)|$$
$$\Rightarrow \qquad = \frac{1}{2} |ac - ab + ab - bc + bc - ac| = 0$$
  
$$\therefore ar(\Delta PQR) = 0$$

Hence, points are collinear.

#### Question 112.

If the point P(m, 3) lies on the line segment joining the points A(-2/5,6) and B(2, 8), find the value of m.

CLICK HERE

🕀 www.studentbro.in

Solution:

Let point P divides AB in ratio k : 1. ation fo Using

and,

 $\Rightarrow$ 

⇒

#### Question 113.

Point P divides the line segment joining the points A(-I, 3) and B(9, 8) such that AP/PB=k/1. If P lies on the line x - y + 2 = 0, find the value of k.

## Solution:

P divides the joining of A(-1, 3) and B(9, 8) such that  $\frac{AP}{AB} = \frac{k}{1}$  i.e. AP : PB = k : 1. Using section formula,

$$\therefore \text{ Coordinates of P are: } \left(\frac{9k-1}{k+1}, \frac{8k+3}{k+1}\right)$$
  
If P lies on  $x - y + 2 = 0$ , then P must satisfy it.  

$$\frac{9k-1}{k+1} - \left(\frac{8k+3}{k+1}\right) + 2 = 0$$
  

$$\Rightarrow \qquad 9k - 1 - 8k - 3 + 2k + 2 = 0$$
  

$$\Rightarrow \qquad 3k - 2 = 0$$
  

$$\Rightarrow \qquad k = \frac{2}{3}$$

#### Question 114.

Find the value of k, if the points A(7, -2), B(5,1) and C(3,2k) are collinear Solution:

If points A(7, -2), B(5, 1) and C(3, 2k) are collinear then, ar  $\triangle ABC = 0$ 

[:: Area of triangle 
$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$$
  
∴ ar  $\triangle ABC = \frac{1}{2} [7(1 - 2k) + 5(2k + 2) + 3(-2 - 1)] = 0$   
⇒  $7 - 14k + 10k + 10 - 9 = 0$   
⇒  $-4k = -8$  ⇒  $k = 2$ 

#### Question 115.

If the points (p, q); (m, n) and (p-m,q-n) are collinear, show that pn = qm Solution:

If P(p,q), Q(m,n), R(p-m,q-n) are collinear then area of triangle formed by them is zero. Hence, ar  $\Delta PQR = 0$ 

$$[\because \text{ Area of triangle} = \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$$

$$\frac{1}{2} [pn - qm + mq - mn - pn + mn + pq - mq - qp + pn] = 0$$

$$\Rightarrow \qquad |pn - qm| = 0$$

$$\Rightarrow \qquad pn - qm = 0$$

$$\Rightarrow \qquad pn = qm$$

CLICK HERE

>>

Hence, proved.

🕀 www.studentbro.in

#### Question 116.

Find the value of k, if the points A(8,1), B(3, -4) and C(2, k) are collinear **Solution:** 

Given points are A(8, 1), B(3, -4) and C(2, k).

As these points are collinear, so the area of triangle formed by these points is zero sq. units.

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$
  

$$\therefore \quad \frac{1}{2} [8(-4-k) + 3(k-1) + 2(1+4)] = 0$$
  

$$\therefore \quad -32 - 8k + 3k - 3 + 10 = 0$$
  

$$-5k - 25 = 0$$
  

$$\therefore \qquad k = -5$$

#### Question 117.

If point P (1/2, y )lies on the line segment joining the points A(3, -5) and B(-7,9) then find the ratio in which P divides AB. Also find the value of y.

## Solution:

Let P divides AB in the ratio k : 1.

$$\therefore \qquad \left(\frac{-7k+3}{k+1}, \frac{9k-5}{k+1}\right) = \left(\frac{1}{2}, y\right) \qquad \dots(i) \qquad A(3, -5) \qquad P\left(\frac{1}{2}, y\right) \qquad B(-7, 9)$$

$$\Rightarrow \qquad \qquad \frac{-7k+3}{k+1} = \frac{1}{2}$$

$$\Rightarrow \qquad -14k+6 = k+1$$

$$\Rightarrow \qquad -15k = -5$$

$$\Rightarrow \qquad \qquad k = \frac{1}{3}$$

$$\therefore \text{ Ratio is } k:1, \text{ i.e. } \frac{1}{3}:1 \Rightarrow 1:3$$

and, using (i), 
$$y = \frac{9k-5}{k+1} = \frac{9 \times \frac{1}{3} - 5}{\frac{1}{3} + 1} = \frac{-6}{4} = \frac{-3}{2} \quad \therefore \quad y = \frac{-3}{2}$$

## Question 118.

Find the value of k for which the points A(9, k), B(4, -2) and C(3, -3) are collinear. **Solution:** 

If points A(9, k), B(4, -2) and C(3, -3) are collinear, so, ar ( $\triangle ABC$ ) = 0 [:: Area of triangle =  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$   $\Rightarrow \frac{1}{2} |9(-2+3) + 4(-3-k) + 3(k+2)| = 0$   $\Rightarrow |9-12-4k+3k+6| = 0$   $\Rightarrow -k = -3$  $\Rightarrow k = 3$ 

### Question 119.

Find the value of k for which the points A(fc, 5), B(0,1) and C(2, -3) are collinear. **Solution:** 

If A(k, 5), B(0, 1), C(2, -3) are collinear then ar  $\triangle ABC = 0$ . [:: Area of triangle =  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$   $\Rightarrow \frac{1}{2} [k(1 + 3) + 0(-3 - 5) + 2(5 - 1)] = 0$   $\Rightarrow | 4k + 8 | = 0$   $\Rightarrow | 4k - 8$  $\Rightarrow | k = -2$ 

CLICK HERE

## Question 120.

Find the value of p for which the points A(-1, 3), B(2,p) and C(5, -1) are collinear. Solution:

If points A(-1, 3), B(2, p) and C(5, -1) are collinear, then ar ( $\triangle ABC$ ) = 0 [:: Area of triangle =  $\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]]$   $\Rightarrow \frac{1}{2} [-1(p+1) + 2(-1-3) + 5(3-p)] = 0$   $\Rightarrow |-p-1-8+15-5p| = 0$   $\Rightarrow 6p = 6$  $\Rightarrow p = 1$ 



